

The future via the past: Effective Field Theory searches for new physics at JADE, LHC, and future colliders

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2025 November 12

Baylor University

- ▶ Medium-sized private R1 university
- ▶ Affiliated with the Baptist Church
- ▶ Central Texas, between Dallas and Austin
- ▶ Chartered in 1845 by the Republic of Texas – oldest university in the state

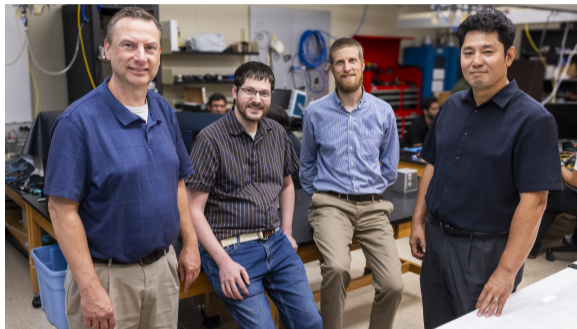


2024 total eclipse passed right across Baylor

Department of Physics and Astronomy

- ▶ 20 faculty, ~50 majors, ~50 grad students
- ▶ Broad range of research:
 - ▶ Astrophysics: observational cosmology, stellar evolution
 - ▶ Space physics: dusty plasmas, hypervelocity impacts
 - ▶ Cosmology, strings, gravity
 - ▶ Ultrafast spectroscopy & nonlinear optics
 - ▶ Surface physics and Raman spectroscopy
 - ▶ Quantum dots, nanoscale fabrication, structure-property relationship
 - ▶ Nonlinear dynamics
 - ▶ Particle theory and lattice QCD
 - ▶ **Experimental particle physics**

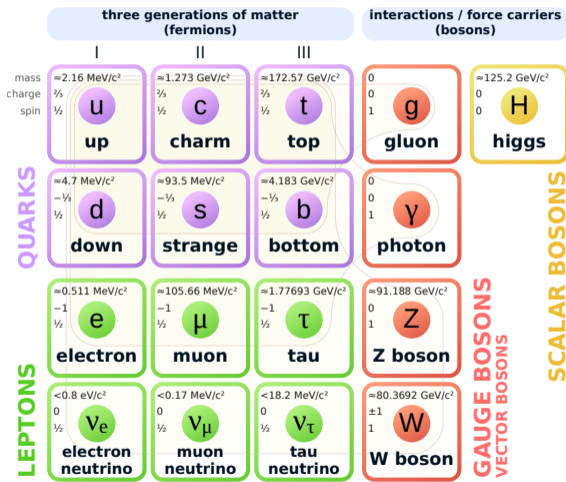
- ▶ Experimental HEP group at Baylor
- ▶ Established 2003 (CDF experiment)
- ▶ Four faculty, 3 postdocs, 6 grad students, ~5 undergrads
- ▶ Working primarily on the CMS experiment
- ▶ Studying Higgs boson, top quark, SUSY, exotica, Effective Field Theory
- ▶ Trigger, data-quality monitoring, reconstruction, hadron calorimeter upgrade and operations, endcap calorimeter upgrade
- ▶ Developing advanced calorimeters for future colliders (CalVision)

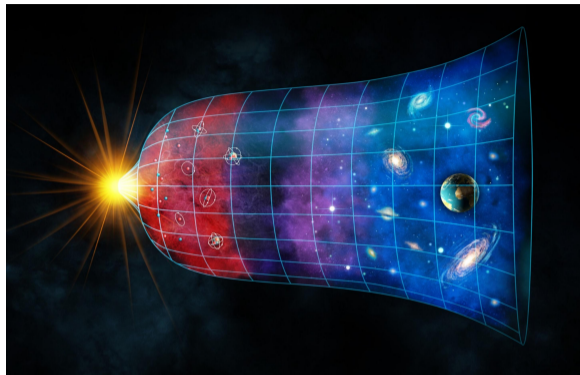


(left to right) Jay Dittmann, JSW, Andrew Brinkerhoff, and Kenichi Hatakeyama

- ▶ The standard model of particle physics is the most successful scientific theory yet
 - ▶ Explains (almost) all phenomena across a huge range of scales
 - ▶ Includes all known fundamental particles
 - ▶ Final predicted particle, the Higgs boson, discovered in 2012
 - ▶ All known interactions except gravity
 - ▶ Has withstood vast array of extremely precise measurements for half a century
 - ▶ Only 19 free parameters

Standard Model of Elementary Particles

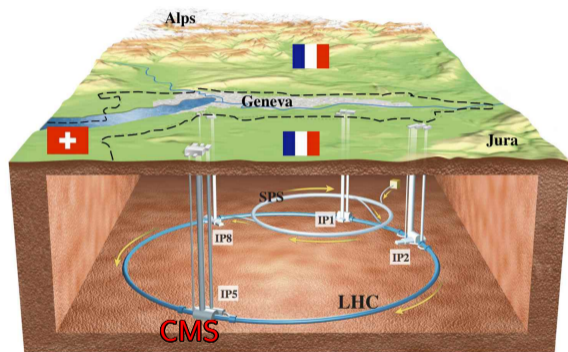




$$\Delta M_{H^2} = -\frac{3y_t^2}{8\pi^2}\Lambda^2$$

- ▶ The SM cannot explain:
 - ▶ Gravity
 - ▶ Cosmic inflation
 - ▶ Dark energy
 - ▶ Dark matter
 - ▶ Fine-tuning of the Higgs boson mass
 - ▶ Strong CP problem
 - ▶ Neutrino masses
- ▶ We know that there is undiscovered physics out there
- ▶ New particles and interactions
- ▶ Why haven't we found them yet?
- ▶ Either large masses or small couplings

- ▶ New particles with small couplings require extremely high precision experiments, e.g.
 - ▶ Muon $g-2$
 - ▶ Mu2e
 - ▶ LZ, LDMX
 - ▶ DUNE, NO ν A
- ▶ New particles with large masses require high energy colliders
 - ▶ LHC: highest energy collider in the world
 - ▶ At CERN, on Swiss-French border
 - ▶ Collides two beams of protons at a center of mass energy of 13.6 TeV
 - ▶ Began operations in 2009
 - ▶ Four experiments: ATLAS, ALICE, Compact Muon Solenoid (CMS), and LHCb



CMS DETECTOR

Total weight : 14,000 tonnes
Overall diameter : 15.0 m
Overall length : 28.7 m
Magnetic field : 3.8 T

STEEL RETURN YOKE
12,500 tonnes

SILICON TRACKERS
Pixel ($100 \times 150 \mu\text{m}$) $\sim 1\text{m}^2$ $\sim 66\text{M}$ channels
Microstrips ($80 \times 180 \mu\text{m}$) $\sim 200\text{m}^2$ $\sim 9.6\text{M}$ channels

SUPERCONDUCTING SOLENOID
Niobium titanium coil carrying $\sim 18,000\text{A}$

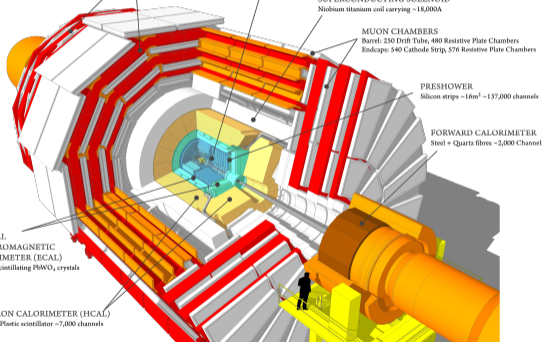
MUON CHAMBERS
Barrel: 250 Drift Tube, 480 Resistive Plate Chambers
Endcap: 540 Cathode Strip, 576 Resistive Plate Chambers

PRESHOWER
Silicon strips $\sim 16\text{m}^2$ $\sim 137,000$ channels

FORWARD CALORIMETER
Steel + Quartz fibres $\sim 2,000$ Channels

CRYSTAL
ELECTROMAGNETIC
CALORIMETER (ECAL)
 $\sim 76,000$ scintillating PbWO_4 crystals

HADRON CALORIMETER (HCAL)
Brass + Plastic scintillator $\sim 7,000$ channels

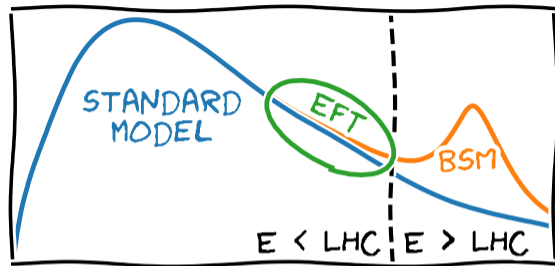


- ▶ CMS is a general-purpose particle detector
- ▶ Total mass 14000 tonnes
- ▶ Position and momentum measured with tracking system, inside 3.8 T solenoid
- ▶ Energy measured with calorimeter (electromagnetic and hadronic)
- ▶ Muons identified by dedicated muon detectors, interspersed with magnet return yoke
- ▶ Sees 40 million events per second
 - ▶ Each event includes tens of proton-proton interactions
 - ▶ Trigger system picks out about 1000 “interesting” events per second

- ▶ So what do we do with this data?
- ▶ Both direct and indirect searches
- ▶ Direct searches look for new particles with mass less than the center-of-mass energy
 - ▶ Require detailed simulation of specific models – computationally expensive
 - ▶ Could miss something if we don't try the right model
 - ▶ If you see something, gain detailed knowledge of the new physics
 - ▶ Like a magnifying glass, to examine things you can reach
- ▶ Indirect searches can stretch to higher masses
 - ▶ Generic description of new physics – **Effective Field Theory**
 - ▶ Only gain generic knowledge from indirect observation
 - ▶ Like binoculars, to spot things you can't get to yet
- ▶ Crucial to do both!



- ▶ Effective Field Theory (EFT) is a model-independent approach to physics beyond the standard model
- ▶ Assume that new physics exists at some scale Λ beyond the current reach of experiments
- ▶ Enumerate all terms in the Lagrangian, ordered by their mass dimension
- ▶ Multiply terms up to some maximum mass dimension by Wilson coefficients
 - ▶ SM corresponds to all coefficients at zero
 - ▶ Small coefficients = small perturbation on SM = low-energy tail of new physics
- ▶ Perfect tool for indirect searches
- ▶ **Just measure Wilson coefficients**



The EFT Lagrangian

$$\mathcal{L} = \mathcal{L}_{\text{SM}} + \sum_{d=5}^{\infty} \sum_i \frac{1}{\Lambda^{d-4}} c_i^{(d)} \mathcal{O}_i^{(d)}$$

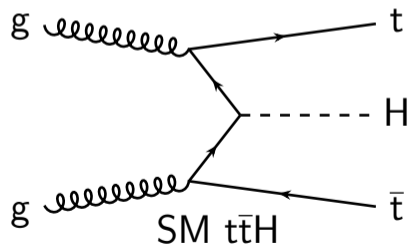
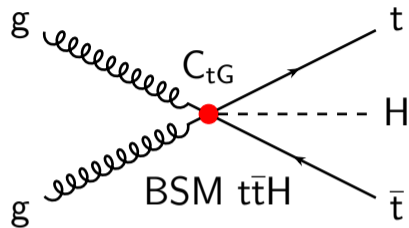
where d is the mass dimension, $c_i^{(d)}$ is a Wilson coefficient, and $\mathcal{O}_i^{(d)}$ is a dimension d operator

- ▶ This is the standard model EFT or “SMEFT”
 - ▶ Provides a common language across measurements, experiments
 - ▶ Facilitates comparison and combination of results
- ▶ Some EFTs other than SMEFT also used in particle physics
 - ▶ Low energy effective field theory used in studies of bottom and charm quarks

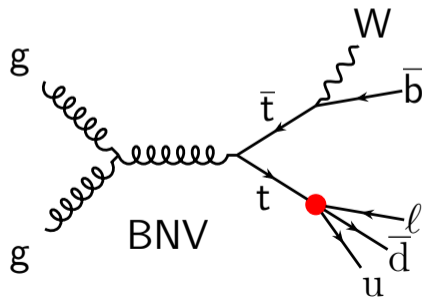
Historical / other EFTs include

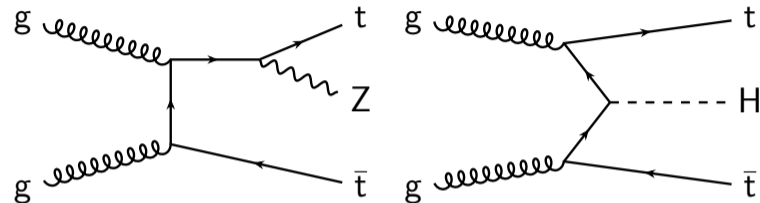
- ▶ Fermi's theory of beta decay
- ▶ BCS theory of superconductivity
- ▶ many others, especially in condensed matter physics

- ▶ Usually look at dimension 6 operators
 - ▶ SM already covers dim 2 and 4
 - ▶ Dim 5 only does neutrino mixing
 - ▶ The fun stuff starts at dim 6
 - ▶ Higher dimensions more suppressed by Λ
- ▶ In total, SMEFT has 2499 dim 6 operators
- ▶ Driven by quark- and lepton-flavor combinatorics
- ▶ Simple assumptions about flavor universality leave us with $O(100)$ operators
- ▶ Most processes only affected by a few dozen at most

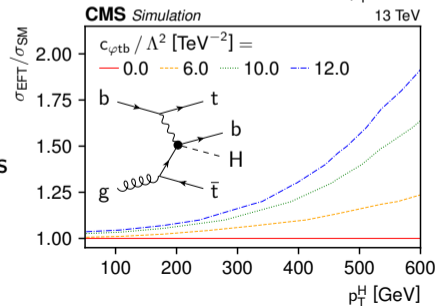
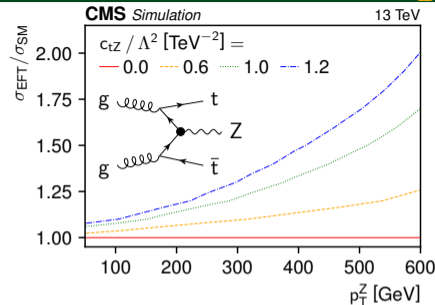


- ▶ Operators may alter rates/spectra for SM processes directly or via interference (diagrams on left)
- ▶ Or allow SM-forbidden processes (below)
- ▶ Make precision measurements and perform searches to constrain Wilson coefficients
- ▶ I'll give an overview of one precision measurement involving top quarks and a Higgs or Z boson

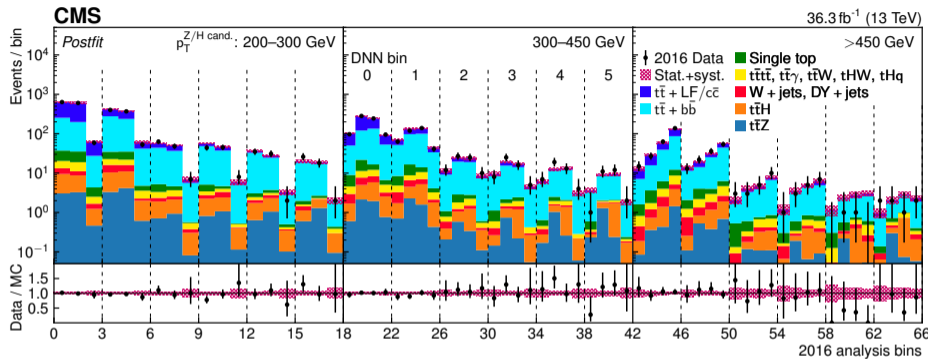




- ▶ Measure $t\bar{t}Z/t\bar{t}H$ when $p_T(Z/H)$ is large
- ▶ EFT effects more pronounced at high $p_T(Z/H)$
- ▶ Select events with one charged lepton, missing p_T , and jets
- ▶ Measure 8 WCs: $c_{t\varphi}$, $c_{\varphi Q}^-$, $c_{\varphi Q}^3$, $c_{\varphi t}$, $c_{\varphi tb}$, c_{tW} , c_{bW} , c_{tZ}

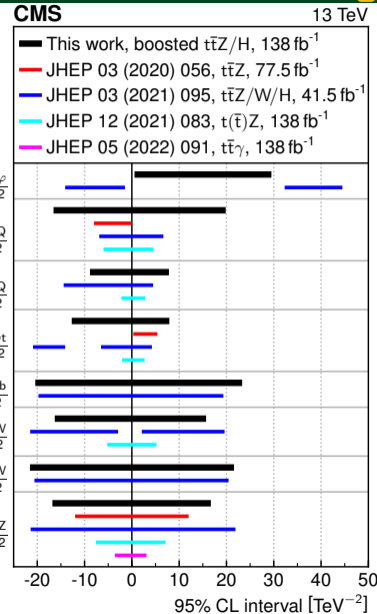
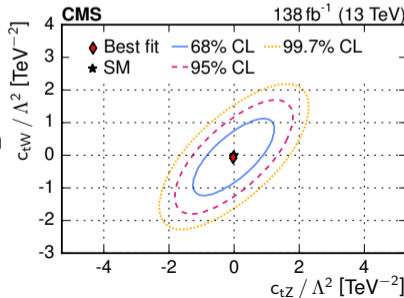
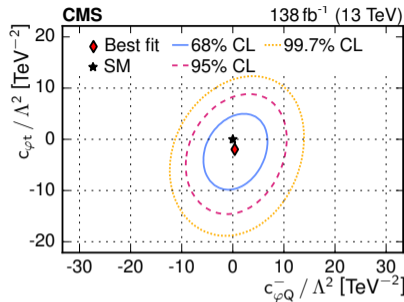


- ▶ 3 large groups $p_T(Z/H)$ bins
- ▶ 6 medium subgroups are NN bins
- ▶ Individual bins are Z/H mass bins
- ▶ No significant deviation from SM expectation
- ▶ Use this to constrain WCs



- ▶ $p_T(Z/H)$ provides EFT sensitivity
- ▶ Neural network (NN) trained to distinguish signals from backgrounds
- ▶ NN score and Z/H mass help control backgrounds
- ▶ Major backgrounds are $t\bar{t} + b\bar{b}$ and $t\bar{t} + \text{jets}$

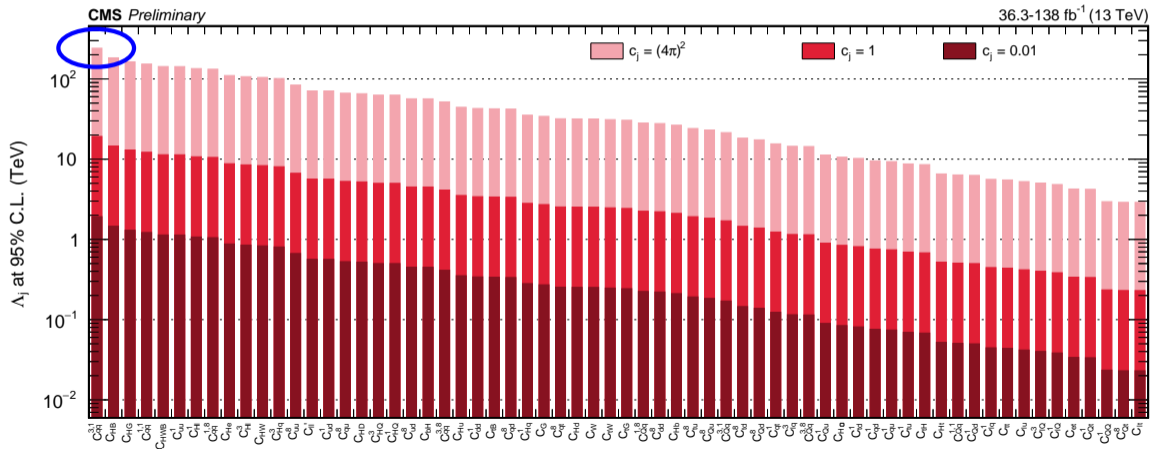
- ▶ Vary the $t\bar{t}Z/H$ signal and $t\bar{t} + b\bar{b}$ background as functions of the WCs
- ▶ Perform 1-D and 2-D likelihood scans for each WC and pair of WCs
- ▶ Consistent with SM (all WCs zero) at 95% CL
- ▶ Comparable sensitivity to other measurements
- ▶ Unique phase space with high-momentum Z/H makes this complementary to other measurements



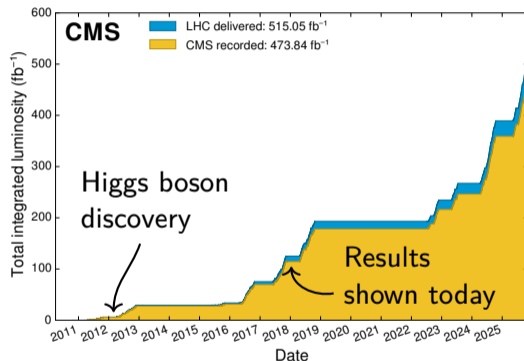
- ▶ Statistical combinations of results are a central promise of EFT
- ▶ Work on combinations only just getting off the ground
 - ▶ First, combinations of top-related measurements, Higgs-related, etc.
 - ▶ Then move to CMS-global combination
 - ▶ Finally combine with other experiments
- ▶ Some pilot efforts in all three of these categories already exist
- ▶ First broad EFT combination from CMS involves 7 CMS measurements, plus electroweak precision observables from the Large Electron Positron collider [CMS-PAS-SMP-24-003]
 - ▶ One Higgs boson
 - ▶ Three with W or Z bosons
 - ▶ Two with top quarks
 - ▶ One with generic jets
- ▶ Constrains 64 Wilson coefficients

- ▶ We always set limits on C/Λ^2 , not C
- ▶ Assume value of C , interpret as limits on new physics scale Λ

- ▶ Best case: for $C_{qq}^{1,3} = (4\pi)^2$, $\Lambda > 229 \text{ TeV}$
- ▶ $\sim 17\times$ the LHC center-of-mass energy
- ▶ Demonstrates reach of indirect searches

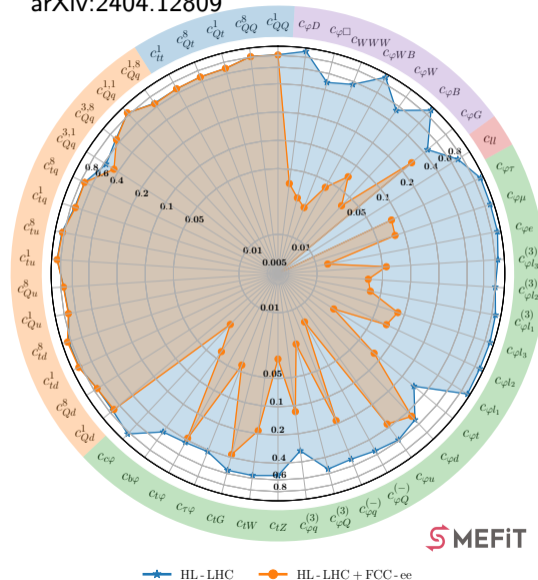


- ▶ Need more data—most EFT results today limited by data set size
- ▶ Already have $> 3.5\times$ as much data
- ▶ Current run will go into July 2026
- ▶ Long shutdown to upgrade LHC, CMS
- ▶ Start High-Luminosity LHC June 2030
- ▶ HL-LHC to run through 2041
- ▶ Will deliver $\sim 10\times$ more data than before
- ▶ Plausible to push Λ sensitivity into **PeV scale!**

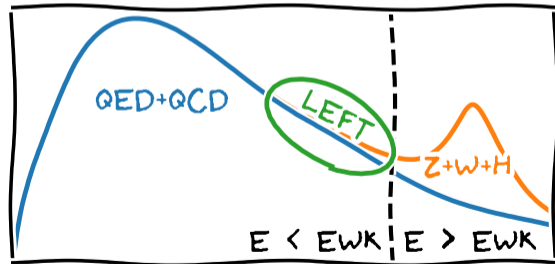
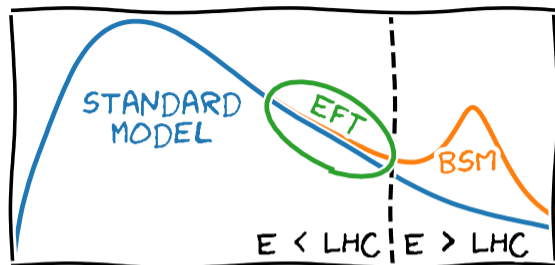


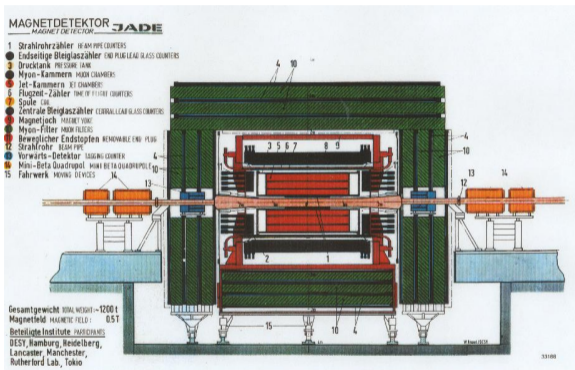
- ▶ FCC-ee: Future Circular Collider e^+e^- is a proposed collider, will run in a new 100 km tunnel at CERN
- ▶ Projected impact on Wilson coefficients (SMEFiT collaboration)
 - ▶ Outer edge shows current SMEFiT bounds
 - ▶ Closer to the center is stronger constraint
- ▶ HL-LHC: substantial improvement over now
- ▶ FCC-ee: massive improvement, except 4-quark operators
- ▶ Will be wonderful to exclude all this phase space for new physics
- ▶ But...we really want to discover something
- ▶ What would it look like to make a discovery via EFT?

Ratio of Uncertainties to SMEFiT3.0 Baseline, $\mathcal{O}(\Lambda^{-4})$, Marginalised
arXiv:2404.12809



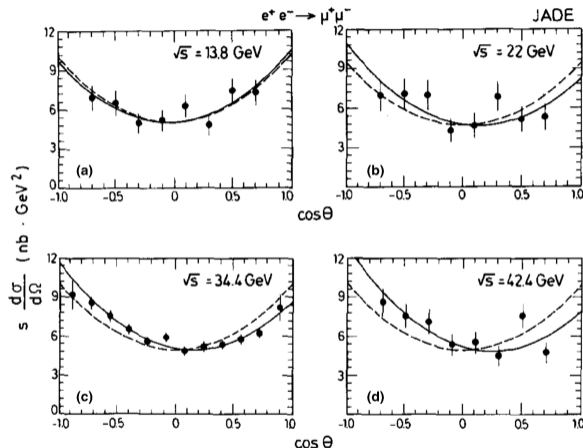
- ▶ Effective Field Theory gives us a way to describe the effects of high-scale physics on low-scale experiments
- ▶ Can be hard to visualize generic BSM
- ▶ Let's treat part of the SM that we're very familiar with as "new" physics
- ▶ Look at data below electroweak scale – look to the past to understand the future
- ▶ Integrate out W , Z , and Higgs bosons (and top quark)
 - ▶ Low-energy Effective Field Theory (LEFT) [JHEP 03 (2018) 016]

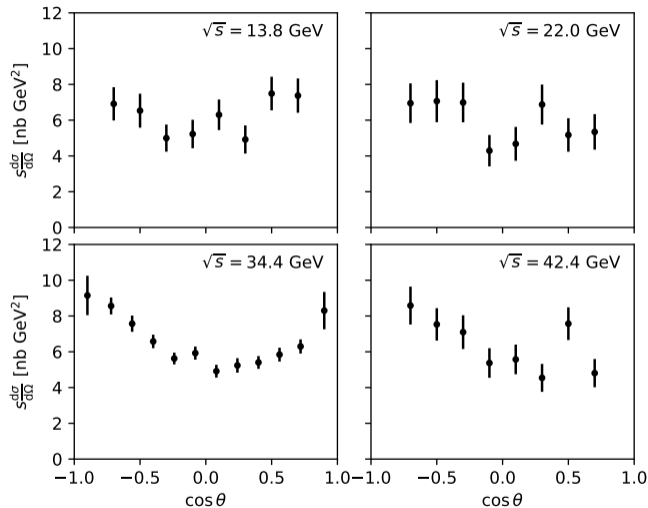




- ▶ JADE was an experiment at the PETRA e^+e^- collider at DESY
- ▶ Discovered the gluon by observing 3 jet events from e^+e^-
- ▶ 1979 – 1986
- ▶ Partly before UA1 and UA2 discovered W and Z
- ▶ Center of mass energies below electroweak scale: roughly 10 to 45 GeV

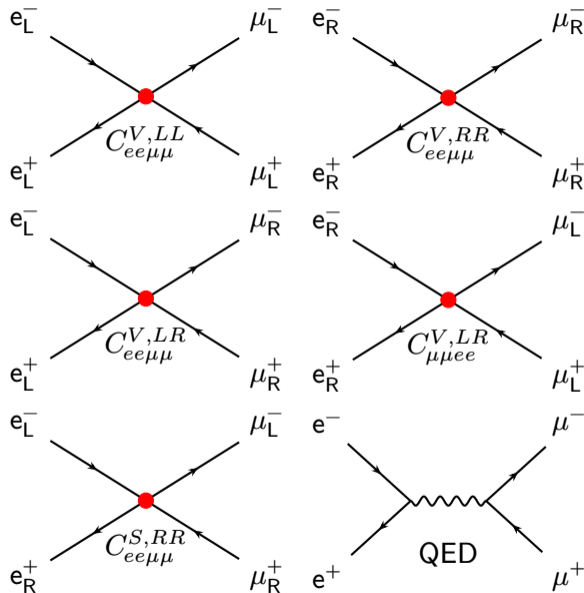
- ▶ JADE also measured $e^+e^- \rightarrow \mu^+\mu^-$
- ▶ Z.Phys.C 26 (1985) 507
- ▶ Muon asymmetry at 4 energies
- ▶ Dashed line QED, solid line EWK
- ▶ Let's apply LEFT to this data and see what we can learn
- ▶ An ahistorical case study
 - ▶ Pretend this is the only data we have:
 - ▶ No UA1/UA2
 - ▶ No neutrino data
 - ▶ Don't even know G_F
 - ▶ What can LEFT tell us about physics beyond QED from JADE alone?





- First, we need to digitize the JADE data
- I used WebPlotDigitizer, but other plot digitizers would work
- Also need to understand binning and normalization
- At 13.8, 22, and 42.4 GeV, 8 bins span $|\cos \theta| < 0.8$: bin size 0.2
- At 34.4, ten bins span $|\cos \theta| < 0.8$: bin size 0.16, plus one bin at each end covering $0.8 < |\cos \theta| < 1.0$
- Plot contains $s \frac{d\sigma}{d\Omega}$, in nb GeV²
- Bin width divided out

- ▶ Now we need to understand what LEFT predicts for this data
- ▶ Relevant operators (excluding CLFV, CPV, and dipole operators):
 - ▶ $C_{ee\mu\mu}^{V,LL}: (\bar{\psi}_{eL}\gamma_\mu\psi_{eL})(\bar{\psi}_{\mu L}\gamma^\mu\psi_{\mu L})$
 - ▶ $C_{ee\mu\mu}^{V,RR}: (\bar{\psi}_{eR}\gamma_\mu\psi_{eR})(\bar{\psi}_{\mu R}\gamma^\mu\psi_{\mu R})$
 - ▶ $C_{ee\mu\mu}^{V,LR}: (\bar{\psi}_{eL}\gamma_\mu\psi_{eL})(\bar{\psi}_{\mu R}\gamma^\mu\psi_{\mu R})$
 - ▶ $C_{\mu\mu ee}^{V,LR}: (\bar{\psi}_{\mu L}\gamma_\mu\psi_{\mu L})(\bar{\psi}_{eR}\gamma^\mu\psi_{eR})$
 - ▶ $C_{ee\mu\mu}^{S,RR}: (\bar{\psi}_{eL}\psi_{eR})(\bar{\psi}_{\mu L}\psi_{\mu R})$
- ▶ Four vector operators, one scalar
- ▶ Vector: like integrating out the Z boson
- ▶ Scalar: like integrating out the Higgs boson
- ▶ Also include QED!



- Pure QED prediction at tree level:

$$\frac{d\sigma}{d\cos\theta} = \frac{\pi\alpha^2}{2s} (1 + \cos^2\theta)$$

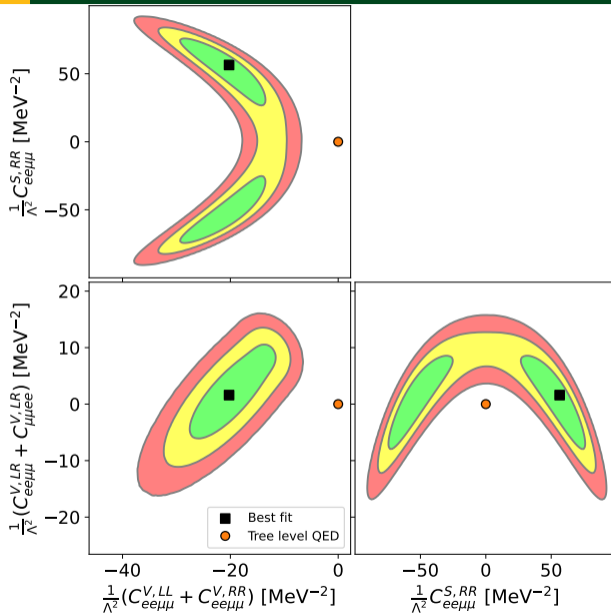
- Tree-level LEFT prediction, up to leading order in EFT:

$$\begin{aligned} \frac{d\sigma}{d\cos\theta} = & \left[\frac{\alpha}{16} \frac{1}{\Lambda^2} \Re(C_{ee\mu\mu}^{V,LL} + C_{ee\mu\mu}^{V,RR} + C_{ee\mu\mu}^{V,LR} + C_{\mu\mu ee}^{V,LR}) + \frac{\pi\alpha^2}{2s} \right] (1 + \cos^2\theta) \\ & + \left[\frac{\alpha}{16} \frac{1}{\Lambda^2} \Re(C_{ee\mu\mu}^{V,LL} + C_{ee\mu\mu}^{V,RR} - C_{ee\mu\mu}^{V,LR} - C_{\mu\mu ee}^{V,LR}) \right] 2\cos\theta \\ & + \frac{1}{128\pi} \frac{s}{\Lambda^4} |C_{ee\mu\mu}^{S,RR}|^2 \end{aligned}$$

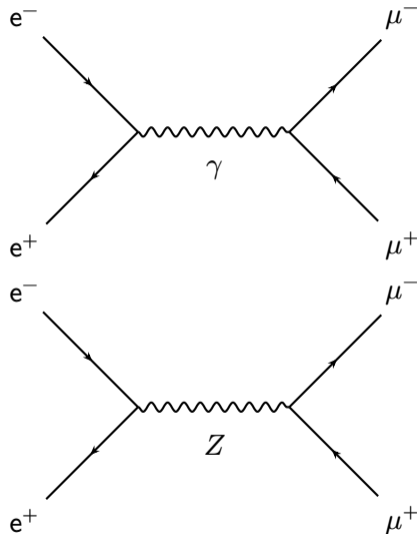
- Now have components $1 + \cos^2\theta$, $2\cos\theta$, and flat
- Only sensitive to some linear combinations of Wilson coefficients:

$$\begin{aligned} \text{► } \Re(C_{ee\mu\mu}^{V,LL} + C_{ee\mu\mu}^{V,RR}) / \Lambda^2 \quad & \text{► } \Re(C_{ee\mu\mu}^{V,LR} + C_{\mu\mu ee}^{V,LR}) / \Lambda^2 \quad & \text{► } |C_{ee\mu\mu}^{S,RR}|^2 / \Lambda^4 \end{aligned}$$

- Flat priors for the WCs
- Integrate cross section in each bin
- Data Gaussian around cross section, width=data error bar
- Use MCMC (pymc5) to sample from posterior
- Plot 68.27, 95.45, and 99.73% credible regions
- Banana-shaped region in 3D
- Very far from QED-only prediction
- **We have used EFT to discover “new” physics!**



- ▶ Great, now what?
- ▶ EFT alone doesn't tell much detail about new physics
- ▶ Talk to model builders
- ▶ Take a specific model, compare to WCs
 - ▶ Don't need to re-analyze data to compare to other models
 - ▶ No model-specific Monte Carlo
- ▶ What do WCs tell about model parameters?
- ▶ Obvious model: electroweak theory
 - ▶ Two relevant parameters: M_W and M_Z
 - ▶ Equivalent: G_F and $\sin^2 \theta_W$
- ▶ Two diagrams: γ and Z



- ▶ Tree level prediction of the electroweak theory:

$$\begin{aligned} \frac{d\sigma}{d\cos\theta} = & \frac{\pi\alpha^2}{2s} (1 + \cos^2\theta) \\ & + \frac{G_F^2 M_Z^4}{\pi} \frac{s}{(s - M_Z^2)^2 + M_Z^2 \Gamma_Z^2} \left[(g_V^2 + g_A^2)^2 (1 + \cos^2\theta) + 8g_V^2 g_A^2 \cos\theta \right] \\ & + \sqrt{2}\alpha G_F M_Z^2 \frac{s - M_Z^2}{(s - M_Z^2)^2 + M_Z^2 \Gamma_Z^2} [g_V^2 (1 + \cos^2\theta) + 2g_A^2 \cos\theta] \end{aligned}$$

- ▶ G_F : Fermi constant
- ▶ M_Z : Z boson mass
- ▶ Γ_Z : Z boson width
- ▶ α : Fine-structure constant
- ▶ g_V : vector coupling of muon/electron to Z , $-\frac{1}{4} + \sin^2\theta_W$
- ▶ g_A : axial-vector coupling of muon/electron to Z , $-\frac{1}{4}$
- ▶ $\sin^2\theta_W$: Weinberg angle

- If we compare the electroweak and LEFT cross sections, we can find electroweak predictions for the WCs
- LEFT cross section is already leading-order expansion in s/Λ^2 , so take leading-order expansion of electroweak cross section (i.e., just set $s \rightarrow 0$):

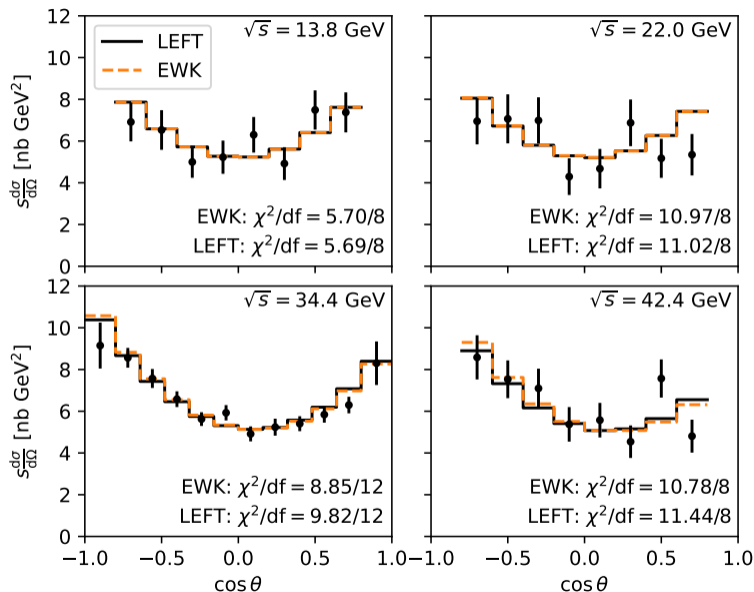
$$\Re(C_{ee\mu\mu}^{V,LL} + C_{ee\mu\mu}^{V,RR})/\Lambda^2 = -8\sqrt{2}G_F \frac{M_Z^2}{M_Z^2 + \Gamma_Z^2} (g_V^2 + g_A^2) \quad (1)$$

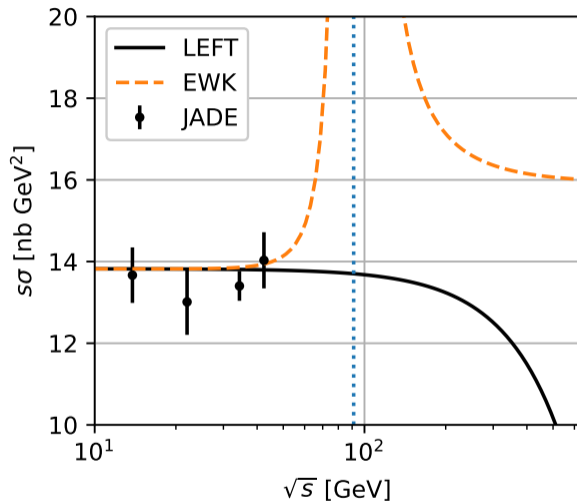
$$\Re(C_{ee\mu\mu}^{V,LR} + C_{\mu\mu ee}^{V,LR})/\Lambda^2 = -8\sqrt{2}G_F \frac{M_Z^2}{M_Z^2 + \Gamma_Z^2} (g_V^2 - g_A^2) \quad (2)$$

$$C_{ee\mu\mu}^{S,RR} = 0 \quad (3)$$

- We can let $\Gamma_Z \rightarrow 0$ to very good approximation
- Then these are just in terms of G_F and $\sin^2 \theta_W$ (via g_V)

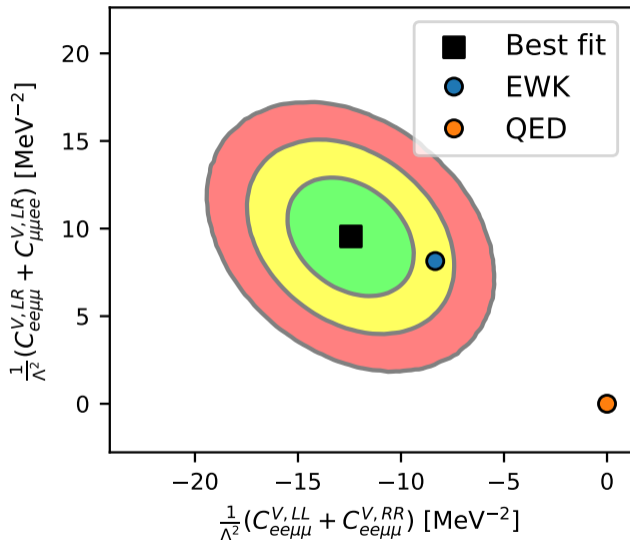
- Compare data to electroweak and LEFT predictions (WCs matched to EWK)
- Generally good description of data
- Electroweak and LEFT predictions very similar, not identical



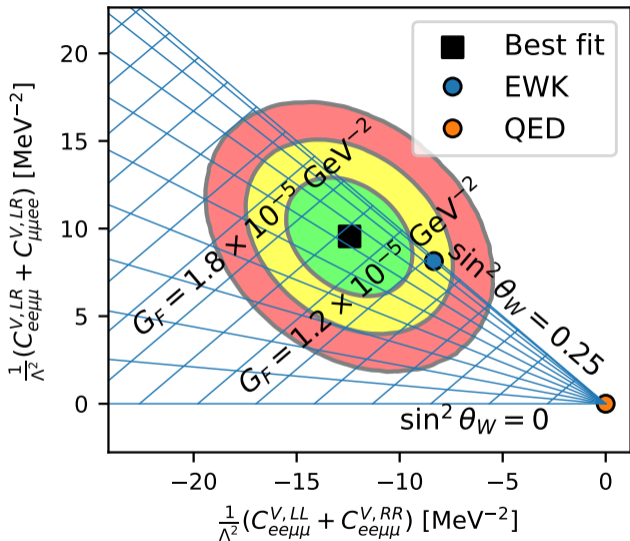


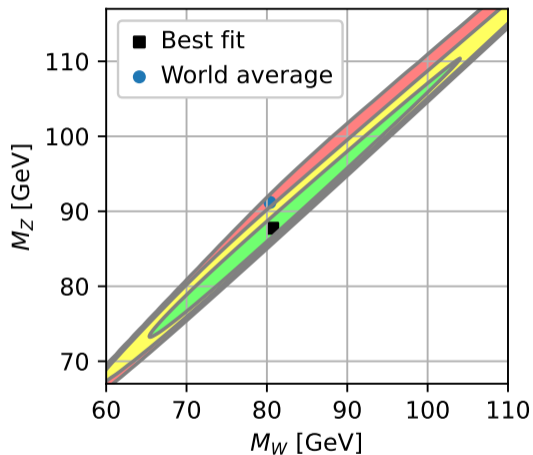
- ▶ Sum data over bins after correcting for bin width, then correct for fiducial region, to get total cross section
- ▶ Compare to electroweak prediction and to LEFT (matched WCs)
- ▶ For JADE energies, LEFT good approximation to electroweak
- ▶ Diverge rapidly closer to Z pole
- ▶ Above Z pole, LEFT will not converge, even with inclusion of arbitrarily high dimension operators

- ▶ What can we say about electroweak parameters from LEFT WCs?
- ▶ First, redo fit with $C_{ee\mu\mu}^{S,RR} = 0$
 - ▶ Equivalent to taking slice through posterior at $C_{ee\mu\mu}^{S,RR} = 0$
- ▶ Plot 2D posterior as function of remaining WCs
- ▶ QED-only still strongly excluded
- ▶ EWK expectation for WCs within 95.45% credible region



- Overlay contours of constant G_F and $\sin^2 \theta_W$
- $G_F = 0$ recovers QED (= infinite M_W, M_Z)
- $\sin^2 \theta_W = 0$ is horizontal
- $\sin^2 \theta_W = 0.25$ is diagonal
- For larger $\sin^2 \theta_W$, turns around and goes back down
 - $\sin^2 \theta_W = 0.5$ is horizontal
 - $\sin^2 \theta_W = 1$ opposite diagonal
 - Posterior is double covered
 - Upper right region impossible (at electroweak tree level)
- Calculate $M_{W,Z}$ from $G_F, \sin^2 \theta_W$
- **We can measure M_W and M_Z !**





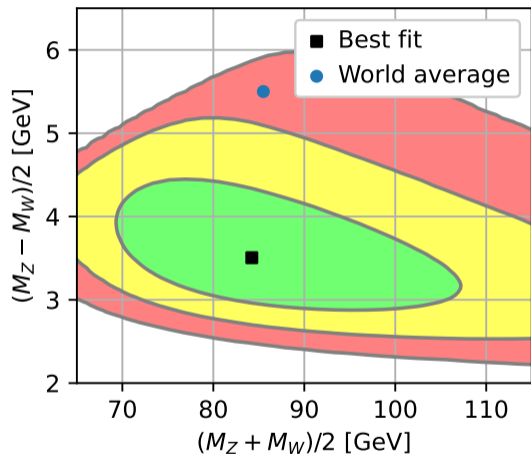
- ▶ For each posterior point in allowed region, compute G_F , $\sin^2 \theta_W$ from WCs
 - ▶ Forbidden region removed, posterior rescaled to total probability of 1
 - ▶ For double-covered region, use $\sin^2 \theta_W < 0.25$

- ▶ Then compute

$$M_W^2 = \frac{\pi\alpha}{\sqrt{2}G_F \sin^2 \theta_W}$$

$$M_Z^2 = \frac{\pi\alpha}{\sqrt{2}G_F (1 - \sin^2 \theta_W) \sin^2 \theta_W}$$

- ▶ Plot posterior as function of M_W , M_Z
- ▶ Looks pretty decent!
- ▶ Let's look more closely



- ▶ Plotting sum vs. diff makes it easier to see
- ▶ Real M_W , M_Z fall outside 95.45% region, inside 99.73% region
- ▶ Lots of room for improvement:
 - ▶ Calculations beyond LO
 - ▶ Radiative corrections to QED
 - ▶ Top-quark loop affects $M_W - M_Z$
 - ▶ Running couplings, esp. α
 - ▶ Better treatment of data uncertainties
- ▶ But still, remarkable that we could get W and Z boson masses from this data through the EFT lens!
- ▶ Would have been enough to guide construction of $Spp\bar{p}S$ or LEP, even without other electroweak constraints available at the time

- ▶ The point is *not* to measure the W and Z masses; we already know those
- ▶ The point *is* that EFT gave us a crude measurement of the “new particle” masses
- ▶ It's very hard to get funding to build a new, higher-energy collider
 - ▶ Especially when we don't even know whether there's anything for it to find
- ▶ But if we had something of this caliber, a $\sim 20\%$ measurement of new particle masses, the (funding) world would be very different

In fairness, none of that was my goal in starting this case study

- ▶ I wanted to develop intuition about the relationship between BSM physics and SMEFT operators
- ▶ Also to better understand how “matching” works
- ▶ But the end result was so much better than the starting plan
- ▶ If we find new physics via EFT, we will learn enough to guide the future of the field towards on-shell discovery
- ▶ “EFT at JADE: a case study”, arXiv:2407.03468.

BACKUP

- ▶ Important note for correct normalization of cross sections: $d\Omega = d\varphi d\cos\theta$
- ▶ Because the cross sections do not depend on φ , $\frac{d\sigma}{d\cos\theta} = \int_0^{2\pi} d\varphi \frac{d\sigma}{d\Omega} = 2\pi \frac{d\sigma}{d\Omega}$
- ▶ The JADE data plots show $\frac{d\sigma}{d\Omega}$, while the analytic tree level cross sections in the slides are given as $\frac{d\sigma}{d\cos\theta}$.
- ▶ Also, to recover physical units nb GeV² from natural units, one has to multiply by $(\hbar c)^2 = 3.893\,793\,72 \times 10^5 \text{ nb GeV}^2$